

MATHEMATICS

CLASS IX

CHAPTER 7: POLYNOMIAL

1. Both $(x - 2)$ and $\left(x - \frac{1}{2}\right)$ are the factors of the polynomial $px^2 + 5x + r$, calculate and write the relation between p and r .

Ans. Let, $f(x) = Px^2 + 5x + r$

Zero of the polynomial $(x - 2)$ is 2 $\therefore x - 2 = 0$ or, $x = 2$

Zero of the polynomial $\left(x - \frac{1}{2}\right)$ is $\frac{1}{2}$, $\therefore x - \frac{1}{2} = 0$ or, $x = \frac{1}{2}$

$\therefore (x - 2)$ and $\left(x - \frac{1}{2}\right)$ are the factors of $f(x)$

$\therefore p(2)^2 + 5(2) + r = 0$ or, $4p + r = -10$

again, $p\left(\frac{1}{2}\right)^2 + 5\left(\frac{1}{2}\right) + r = 0$

or, $\frac{p}{4} + \frac{5}{2} + r = 0$ or, $p + 4r = -10$

$\therefore 4p + r = p + 4r$ or, $3p = 3r$ or, $p = r$

2. Find the values of a and b if $x^2 - 4$ is a factor of the polynomial $ax^4 + 2x^3 - 3x^2 + bx - 4$.

Ans. Let, $f(x) = ax^4 + 2x^3 - 3x^2 + bx - 4$

$\therefore (x^2 - 4)$ is a factor of $f(x)$

$\therefore (x - 2)$ and $(x + 2)$ both are factors of $f(x)$

$\therefore f(2) = 0$ and $f(-2) = 0$

if $f(2) = 0$ then $16a + 16 - 12 + 2b - 4 = 0$ or, $16a + 2b = 0$ or, $8a + b = 0$

Again, if $f(-2) = 0$ then $16a - 16 - 12 - 2b - 4 = 0$ or, $16a - 2b = 32$ or, $8a - b = 16$

$$8a + b = 0$$

$$8a - b = 16$$

$$(+), 16a = 16$$

$$\text{or, } a = 1$$

$\therefore 8(1) + b = 0$ or, $b = -8$

$\therefore a = 1, b = -8$

3. If the two polynomials $x^3 + 2x^2 - px - 7$ and $x^3 + px^2 - 12x + 6$ are divided by $(x+1)$ and $(x-2)$ respectively then the remainders R_1 and R_2 are obtained respectively and if $2R_1 + R_2 = 6$, then find the value of p .

Ans. Let, $f(x) = x^3 + 2x^2 - px - 7$ and $g(x) = x^3 + px^2 - 12x + 6$

If $f(x)$ and $g(x)$ are divided by $(x+1)$ and $(x-2)$ then remainders will be R_1 and R_2 .

$$\therefore f(-1) = (-1)^3 + 2(-1)^2 - p(-1) - 7 = R_1$$

$$\text{or, } -1 + 2 + p - 7 = R_1$$

$$\text{or, } p - 6 = R_1$$

Again, $g(2) = 2^3 + p(2)^2 - 12(2) + 6 = R_2$

$$\text{or, } 8 + 4p - 24 + 6 = R_2$$

$$\text{or, } 4p - 10 = R_2$$

Again, $2R_1 + R_2 = 6$

$$\text{or, } 2(p - 6) + 4p - 10 = 6$$

$$\text{or, } 6p = 28$$

$$\text{or, } p = \frac{28}{6}$$

$$\text{or, } p = \frac{14}{3} = 4\frac{2}{3}$$

\therefore The value of p is $4\frac{2}{3}$.